

Teltest Electronics

GPS Position Solution Calculations $k := 0..0$ k is the epoch $sv := 0..3$ sv is the satellite $\chi := \text{READPRN(EPHEM11)}$ $\rho := \text{READPRN(PRANGE11)}$ $t_s := \rho_{1,8}$ $t_f := \rho_{1,9} \cdot 10^{-9}$ $tl := t_s + t_f$ $tl = 1.568 \times 10^5$ $SC := -1$

$$tsv_{sv} := \rho_{sv,2} \text{ s} \quad tsvf_{sv} := \rho_{sv,3} \cdot 10^{-9} \text{ s} \quad tsv_{sv} := tsv_{sv} + tsvf_{sv} \quad x_{toc_{sv}} := \chi_{sv,6} \cdot K2p4 \quad t_{sv} := tsv_{sv} - (\chi_{sv,6} \cdot K2p4) \quad tsv_{sv} := tsv_{sv} - \left[(\chi_{sv,9} \cdot K2m31) + t_{sv} \cdot (\chi_{sv,8} \cdot K2m43) + (t_{sv})^2 \cdot (\chi_{sv,7} \cdot K2m55) \right] \quad toe_{sv} := \chi_{sv,15} \cdot K2p4$$

$$M_{sv} := -\chi_{sv,12} \cdot K\pi2m31 \text{ rad} \quad e_{sv} := \chi_{sv,13} \cdot K2m33 \quad A_{2,sv} := \chi_{sv,14} \cdot K2m \sqrt{m} \quad \Delta r_{sv} := F \cdot e_{sv} \cdot A_{2,sv} \cdot \sin(M_{sv}) \quad A_{sv} := (A_{2,sv})^2 \quad n_{o,sv} := \sqrt{\frac{\mu}{(A_{sv})^3}} \quad n_{sv} := n_{o,sv} + (\chi_{sv,11} \cdot K\pi2m43)$$

$$t_{sv} := tsv_{sv} - toe_{sv} \quad M_{sv} := M_{sv} + (t_{sv} - \Delta r_{sv}) \cdot n_{sv} \quad E := M \quad \Delta := .1 \quad Err_{sv} := \frac{\Delta \cdot (M_{sv} - E_{sv} + e_{sv} \cdot \sin(E_{sv}))}{\Delta + e_{sv} \cdot (\sin(E_{sv}) - \sin(E_{sv} + \Delta))} \quad \Delta_{sv} := \frac{Err_{sv}}{10} \quad E_{sv} := Err_{sv} + E_{sv} \quad Err_{sv} := \frac{\Delta_{sv} \cdot (M_{sv} - E_{sv} + e_{sv} \cdot \sin(E_{sv}))}{\Delta_{sv} + e_{sv} \cdot (\sin(E_{sv}) - \sin(E_{sv} + \Delta_{sv}))} \quad \Delta_{sv} := \frac{Err_{sv}}{10} \quad E_{sv} := Err_{sv} + E_{sv}$$

$$Err_{sv} := \frac{\Delta_{sv} \cdot (M_{sv} - E_{sv} + e_{sv} \cdot \sin(E_{sv}))}{\Delta_{sv} + e_{sv} \cdot (\sin(E_{sv}) - \sin(E_{sv} + \Delta_{sv}))} \quad E_{sv} := Err_{sv} + E_{sv} \quad Err_{sv} := E_{sv} - M_{sv} - e_{sv} \cdot \sin(E_{sv}) \quad \cos E_{sv} := \cos(E_{sv}) \cdot \sin E_{sv} := \sin(E_{sv}) \quad v_{sv} := \text{atan} \left[\left(\frac{1 + e_{sv}}{1 - e_{sv}} \right) \cdot \tan \left(\frac{E_{sv}}{2} \right) \right] \cdot 2 \quad \Delta r_{sv} := F \cdot e_{sv} \cdot A_{2,sv} \cdot \sin E_{sv} \quad tsv_{sv} := tsv_{sv} - \Delta r_{sv}$$

$$\Phi_{sv} := v_{sv} - \chi_{sv,18} \cdot K\pi2m31 \cdot SC \quad \sin 2\Phi_{sv} := \sin(2 \cdot \Phi_{sv}) \quad \cos 2\Phi_{sv} := \cos(2 \cdot \Phi_{sv}) \quad u_{sv} := \Phi_{sv} + (-\chi_{sv,24} \cdot K2m29 \cdot SC \cdot \cos 2\Phi_{sv} + \chi_{sv,23} \cdot K2m29 \cdot \sin 2\Phi_{sv}) \quad r_{sv} := A_{sv} \left(1 - e_{sv} \cdot \cos E_{sv} \right) + (\chi_{sv,22} \cdot K2m5 \cdot \cos 2\Phi_{sv} - \chi_{sv,21} \cdot K2m5 \cdot SC \cdot \sin 2\Phi_{sv})$$

$$x'_{sv} := r_{sv} \cdot \cos(u_{sv}) \quad y'_{sv} := r_{sv} \cdot \sin(u_{sv}) \quad i_{sv} := \chi_{sv,17} \cdot K\pi2m31 + (\chi_{sv,26} \cdot K2m29 \cdot \cos 2\Phi_{sv} - \chi_{sv,25} \cdot K2m29 \cdot SC \cdot \sin 2\Phi_{sv}) + -\chi_{sv,20} \cdot K\pi2m43 \cdot SC \cdot t_{sv} \quad \Omega_{sv} := [-\chi_{sv,16} \cdot K\pi2m31 \cdot SC + (-\chi_{sv,19} \cdot K\pi2m43 \cdot SC - \Omega \cdot \dot{dote}) \cdot t_{sv}] - \Omega \cdot \dot{dote} \cdot toe_{sv}$$

$$\cos \Omega_{sv} := \cos(\Omega_{sv}) \quad \sin \Omega_{sv} := \sin(\Omega_{sv}) \quad \cos i_{sv} := \cos(i_{sv}) \quad \sin i_{sv} := \sin(i_{sv}) \quad x_{sv} := x'_{sv} \cdot \cos \Omega_{sv} - y'_{sv} \cdot \cos i_{sv} \cdot \sin \Omega_{sv} \quad y_{sv} := x'_{sv} \cdot \sin \Omega_{sv} + y'_{sv} \cdot \cos i_{sv} \cdot \cos \Omega_{sv} \quad z_{sv} := y'_{sv} \cdot \sin i_{sv} \quad \text{range}_{sv} := \sqrt{(x_{sv})^2 + (y_{sv})^2 + (z_{sv})^2}$$

$$x'' := 976932.741 \quad y'' := -0 - 5050398.949 \quad z'' := 3758625.511 \quad \phi'' := 36.3383141667 \quad \lambda'' := -79.0521030556 \quad h'' := 217.07$$

$$tpr_{sv} := (tl - tsv_{sv}) \quad yi := y \cdot i \quad rs_{sv} := |x_{sv} + yi_{sv}| \quad \theta_{sv} := \arg(x_{sv} + yi_{sv}) \quad \phi := \theta - \Omega \cdot \dot{dote} \cdot tpr \quad x_{sv} := rs_{sv} \cdot \cos(\phi_{sv}) \quad y_{sv} := rs_{sv} \cdot \sin(\phi_{sv}) \quad \text{Compensation for earth rotation during transmission}$$

Pseudorange Solution $j := 0..3$ $sv := 0..3$ $k := 0$ $j1 := 0..5$ $i := 0..3$ $X_j := x_{j+k}$ $Y_j := y_{j+k}$ $Z_j := z_{j+k}$ Satellite position

$$\psi''_{sv} := tpr_{sv} \cdot \text{SOL} \quad \psi_j := \psi''_{j+k} \quad x'_{r'} := x'' \quad y'_{r'} := y'' \quad z'_{r'} := z''$$

$$x_0 := x'_{r'} \quad y_0 := y'_{r'} \quad z_0 := z'_{r'} \quad c\Delta t_0 := 0 \quad \psi'_{i'} := \sqrt{(X_i - x_0)^2 + (Y_i - y_0)^2 + (Z_i - z_0)^2} + c\Delta t_0 \quad \text{Determine range vectors for approximate position.}$$

$$\xi \psi x_i := \frac{-(X_i - x_0)}{\psi'_{i'}} \quad \xi \psi y_i := \frac{-(Y_i - y_0)}{\psi'_{i'}} \quad \xi \psi z_i := \frac{-(Z_i - z_0)}{\psi'_{i'}} \quad M'_{i,0} := \xi \psi x_i \quad M'_{i,1} := \xi \psi y_i \quad M'_{i,2} := \xi \psi z_i \quad M'_{i,3} := 1 \quad \delta E := M'^{-1} \cdot (\psi - \psi')$$

$$\delta E = \begin{pmatrix} 0.1346 \\ 1.446 \\ 0.1917 \\ -0.8037 \end{pmatrix} \quad x'' := x_0 + \delta E_0 \quad y'' := y_0 + \delta E_1 \quad z'' := z_0 + \delta E_2 \quad c\Delta t := c\Delta t_0 + \delta E_3 \quad \psi'' = \begin{pmatrix} 2.339 \times 10^7 \\ 2.242 \times 10^7 \\ 2.37 \times 10^7 \\ 2.193 \times 10^7 \end{pmatrix} \quad \psi = \begin{pmatrix} 2.339 \times 10^7 \\ 2.242 \times 10^7 \\ 2.37 \times 10^7 \\ 2.193 \times 10^7 \end{pmatrix}$$

$$x'' = 9.76932875592941 \times 10^5 \quad y'' = -5.05039750297842 \times 10^6 \quad z'' = 3.7586257 \times 10^6 \quad c\Delta t = -0.804 \quad \text{Error} := \sqrt{(x'_{r'} - x'')^2 + (y'_{r'} - y'')^2 + (z'_{r'} - z'')^2} = 1.465$$

$$e'x := x'_{r'} - x'' \quad e'y := y'_{r'} - y'' \quad e'z := z'_{r'} - z'' \quad e'z = -0.192$$

$$\text{Ft'Mtr} := \frac{1}{.3048} \quad e_2 := \frac{a^2 - b^2}{a^2} \quad e'2 := \frac{a^2 - b^2}{b^2} \quad p := \sqrt{(x'')^2 + (y'')^2} \quad \theta := \text{atan} \left(\frac{z'' \cdot a}{p \cdot b} \right) \quad \phi := \text{atan} \left(\frac{z'' + e'2 \cdot b \cdot \sin(\theta)^3}{p - e_2 \cdot a \cdot \cos(\theta)^3} \right) \quad \lambda := \text{atan} \left(\frac{y''}{x''} \right) \quad N := \frac{a^2}{\sqrt{a^2 \cdot \cos(\phi)^2 + b^2 \cdot \sin(\phi)^2}} \quad h := \frac{p}{\cos(\phi)} - N \quad \phi \cdot \frac{180}{\pi} = 36.338323 \quad \lambda \cdot \frac{180}{\pi} = -79.052099$$

$$h = 216.03 \quad h \cdot \text{Ft'Mtr} = 708.762$$

$$\left(\phi \cdot \frac{180}{\pi} - \phi'' \right) \cdot 3632 \cdot 10^6 \cdot .3048 = 0.978 \quad \left(\lambda \cdot \frac{180}{\pi} - \lambda'' \right) \cdot 2946 \cdot 10^6 \cdot .3048 = 0.407 \quad h - h'' = -1.039$$